POSSIBLE WORLDS

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It is impossible to talk about programming "paradigms" without bringing Object Oriented (OO) programming to mind. The question therefore arises, is there any relationship between Indexical Programming and OO programming.

1. Objects as Filters

Explanations of OO often take as their starting point a model of computation in which objects with internal states send messages to each other. This sounds a lot like the "naive" dataflow model of old (stream-only) lucid, and in fact many simple object/message algorithms can be coded in lucid. The basic idea is that the objects with internal states correspond to (instances of) nonpointwise functions; that the messages are datons sent along the pipes from producer to consumer.

As a simple example, the good old running average program

\[
\text{avg}(X) = T/N \\
\text{where} \\
T = 0 \text{ fby } T + X; \\
N = 0 \text{ fby } N + 1; \\
\text{end}
\]

takes a stream of numbers and produces a corresponding stream of averages-to-date. We can think of each input or output daton as being a one parameter message. T and N are then internal instance variables updated every time a message is handled. (Assume 0/0 yields an error object).

Of course a more "idiomatic" OO treatment of averages would look a bit different. There would be separate messages for registering a new number, for accessing the current average, and for resetting the object. The messages might be look like

```
ADD:23
AVG
RESET
```

One way to capture this in old Lucid (in fact, in pLucid) is to write a filter whose input stream is messages of this type coded, say, as lists. The input stream might begin

```
[RESET] [ADD 23] [ADD 11] [AVG] [ADD 2] [AVG] [RESET] ...
```

in which case the output stream would begin

```
17, 13, ...
```

Here is a pLucid filter which corresponds to this object:

```
\text{avg}(N) = T/N \text{ whenever command eq "AVG"} \\
\text{where} \\
\text{command} = \text{head}(N); \text{param} = \text{head}(\text{tail}(N)); \\
T = \text{case} \text{command} \text{ of}
```

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"RESET": 0;
"ADD"  : T+param;
"AVG"  : T;
end;

N = case command of
  "RESET": 0;
  "ADD"  : T+1;
  "AVG"  : T;
end;

Of course, a native Lucid programmer might express the same idea in a somewhat different way - say, by eliminating lists and making avg a filter with two arguments, command and param. But the correspondence is still pretty close, and the style is practical - most of the old pLucid screen editor was structures along these lines.

We can therefore find Lucid analogs of objects (namely, filters) and messages (namely, datons). We can even regard the definition of a filter as a class, and the particular calls (with particular actual parameters) as instances of the definition.

Do we have OO programming? In my opinion, not at all. We are missing the fundamental ingredient: inheritance.

For example, suppose we wanted to define a class of more elaborate average-calculators, which have extra internal memory (say, to store a running maximum and minimum) and respond to extra messages to display these values. In an OO language we can declare the new class to be a subclass of the existing one, and inherit all the code for dealing with the messages already described. In pLucid, however, we have to clone the definition and hack it - by adding extra definitions and extra alternatives to the case statements. We have to go through the same procedure in more conventional OO languages (such as C), and have therefore the real advantages of OO are still out of reach - even though we have (analogies of) objects, messages and classes.

2. The Software Version Problem

If we want to find a relationship between IP and OO, we should look first of all for some in connection between inheritance and IP.

There is in fact a such a connection, but it was not uncovered in the obvious way, by adding inheritance to an Indexical language. Instead, it grew out of an (initially ad hoc) attempt by the authors to manage a family of prototype implementations of various indexical systems.

Originally, Indexical programming meant programming in One Big Language (Lucid). Implementing IP therefore meant implementing the language. Soon after the publication of the Lucid Book, however, we gave up the attempt and began developing a whole family of languages and systems based on indexical logic. Indexical Lucid is still the most prominent member of this family, but not the only one. Contributions to this and recent ISLIPs give some idea of the diversity which has already apparent in the Indexical family - spreadsheets, logic programming, attribute grammars, higher order languages, and so on.

One great disadvantage of having a family of systems is that you need a family of implementations. Each single paradigm has many variations - temporal logic programming with branching time, or with user-defined dimensions, multi-dimensional spreadsheets, infinite branching time, etc. Some of these variants may be more useful than others, but we may never know which are the useful ones until we try them out.

We would obviously need whole regiments of research assistants to produce separate implementations, even prototype implementations, for all these possibilities. Yet there should be no need to produce separate implementations, because these systems rally are members of a family, and have strong family resemblance. Instead, we can (incrementally) build a family of implementations in which related members share code which
implements common features. For example, all the spreadsheet systems might share the display procedures, and all the Lucid-like functional languages would share the code for implementing branching time.

In other words, the alternative approach is to view the various implementations as versions (variants) of a single piece of software. We therefore need an approach to version management and configuration which allows code sharing between versions. Obviously, this is an important problem not limited to software which implements indexical systems. In fact almost all important commercial products (computers, copiers, airplanes, automobiles, lately even books and newspapers) exist in versions. The control and configuration of the related software and documentation is already serious problem.

3. Versions as Possible Worlds

The indexical approach to version control, which was worked out and formalized in [P W], is based on two simple observations.

The first is that a family of variants of a piece of software can be thought of as an intension, one which varies over a context space whose possible worlds are the particular versions.

The second observation is that a piece of software is the result of combining its components, and that this combination process is a pointwise operation. In other words, we configure the (say) french version of a word-processor by assembling the french versions of its basic components.

These observations are, by themselves, not much help, because they seem to rule out sharing between related versions. Most likely (especially if the software is designed) there will only be a few modules for which the french version is different from the standard one. It is wasteful and error-prone to require the programmer to produce separate french copies of every module.

Instead, we can establish a default convention: if no separate french version of a module M can be found, then the french version of M (the value of M at the french world) is the same as its standard value (its value at the vanilla world). Conceptually, then, M is still an intension with an extension at each world; but the programmer does not actually have to create separate labeled copies of each extension.

The configuration process is only slightly more complicated. To configure the french version, we assemble all the required modules, in each case taking the one labeled french if it exists, otherwise taking the one labeled as standard.

The principle involved becomes clear once we introduce subversions; for example, with french of french, which (along with, say, german and italian) is a subversion of standard. When configuring the frenchach module, to find an explicit frenchwe look for a separate french version; and if that is not available either, we take the standard version.

4. Version Inheritance

The principle is that if there is a copy of a module M labeled with a version alpha, but none labeled with immediate subversion beta, then M sub beta is taken to be equal to M sub alpha. In other words, by default the beta version of the whole system inherits its components from those of version alpha. In general, to configure version alpha of the system, we examine, for each module M, the set of all subversions gamma of alpha for which a labeled copy of M exists (we call these gamma the relevant versions of M). If this set has a least element (least in the subversion ordering) then we take that version of M; otherwise there is an error condition. We can summarize the procedure by saying that we assemble system by choosing, for each module, the most relevant version of that module.

In [PW] we describe a simple version management system (Lemur) for C software based on the indexical approach. Lemur allows sharing of object code as well: it keeps track of the versions used in compiling a .o file, and attaches the appropriate tag. The system allows multiple inheritance: the sum alpha+beta of versions is a subversion of both alpha and beta. Sums are used to recombine separate versions. For example, the french+fast version is the one which is both french and fast. When combining the french and
fast versions, the programmers have to consider only those modules which exist in both versions. In these cases, it is necessary to produce an explicit french-fast version, for otherwise configuration will fail (neither the french nor the fast will be the most relevant).

5. Program Intensions

The basic idea behind the Lemur approach is to use a partially ordered context space and an inheritance rule as the basis of an economical representation of an intension. The same idea can be applied in other systems in which the program text itself is not monolithic but varies over a context space.

In a spreadsheet program, for example, the definition of the sheet S is given by a whole array of separate expressions, one for each point in the context space. And we have already seen examples where this is uneconomical because all the formulas (say, in a particular row) are identical. We can avoid this problem by introducing extra context points which stand for entire classes of cells, and allow the user to give expressions for these classes which will be inherited by the cells in each class.

For example, we can add class-contexts for each row and each column, and one for the entire sheet (with subset ordering). Then to calculate the value at a particular cell, we first check if there is an expression in that particular cell. If there is we evaluate it, otherwise we look for an expression attached to the row or column in which the cell appears. If there is (one), we evaluate it, otherwise look for the generic (default) expression attached to the whole sheet. Clearly multiple inheritance arises again, when the classes (considered as sets of cells) overlap. We could forbid them; or we could require that at the point where they overlap, the expressions have the same value.

Context inheritance also works well with attribute grammars, where typically many productions (such as those involving arithmetic operations) all have identical definitions.

6. The Revised Analogy

In this revised analogy, the objects of OO correspond to the contexts or possible worlds of the intensional model. The messages correspond to demands for the values of particular variables - the variables are the messages. The methods of OO correspond to the defining expressions for the variables. If there is a defining expression already entered at the demanded context, eduction proceeds in the normal way, by evaluating the expression at the context. If there is no expression at the context, we begin searching up the inheritance hierarchy - with the added context points corresponding to classes.

7. Indexical OO Versioning

This indexical view of OO offers some intriguing possibilities. One big problem with OO software is versioning. The problem is that a newer version may change methods found part way up in the inheritance hierarchy. Worse yet, we may want to change the inheritance ordering in a newer version.

A possible solution lies in adapting the Lemur approach to versioning to our indexical model of OO. A message (demand) would be indexed by two coordinates: one to specify the object, the other to specify the version. Both these dimensions have an inheritance order, but it is relatively simple to combine them so that the search for methods proceeds through the new version of the hierarchy, and uses the new versions of the appropriate methods.